

# Physics-Informed Deep Learning to Infer Radiative Fluxes

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## 1 Introduction

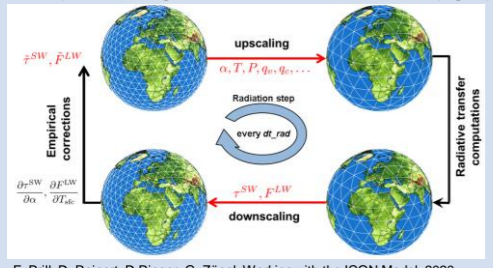
Because of the computational demands, many weather centers use a **reduced spatial grid (fig. 1)** and reduced temporal frequency for radiative transfer calculations in their forecast models.

In this project, we contribute to the discussion on **how to incorporate physical constraints into an ML-based radiative parameterization**, whether to predict radiative flux or its convergence (i.e. heating rates), and how different **neural network (NN)** designs (MLP, **Unet (fig. 2)**) and input features normalization affect prediction performance.

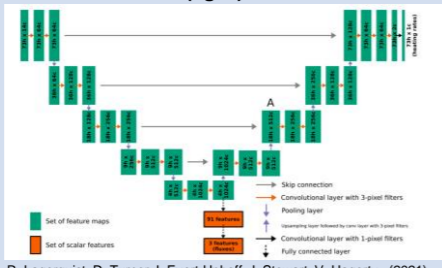
A **random forest (RF)** is used as a baseline method, with ECMWF model **ecRad**, the operational radiation in the **ICON** climate model, used for training. The RF is not affected by the **top-of-atmosphere (TOA)** bias found in all NNs tested. At lower atmospheric levels, the RF is able to compete with the NNs, but its memory requirements become prohibitive.

For a fixed memory size, most NNs outperform the RF except at TOA. Introducing physical constraints into ML design **by penalizing the NNs via heating rates** seems promising.

Computational grid for the radiation in ICON (fig. 1)

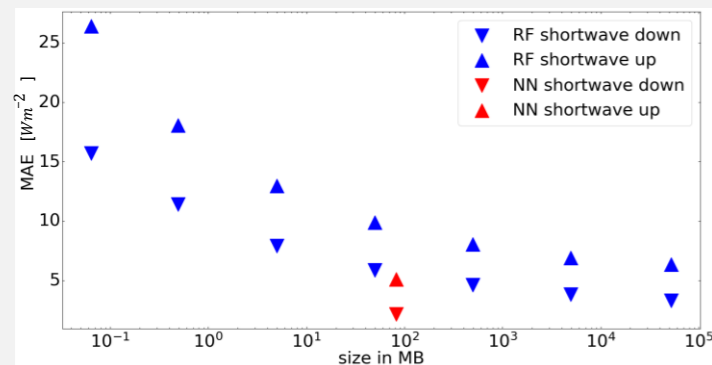


UNet architecture (fig. 2)



## 2 Random Forest size limitations

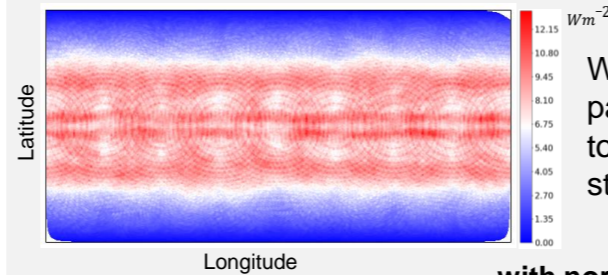
Mean Absolute Error (MAE) of the RF against its size in MB:



The RF can compete with NNs but its size in MB becomes prohibitive

## 3 Random Forest normalization

Shortwave prediction without normalization:



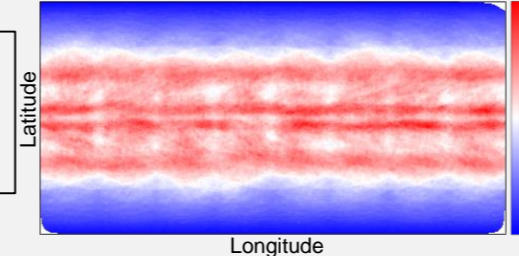
We observe discrete patterns in the error due to the piecewise constant structure of the RF.

Output normalization:

We divide the shortwave fluxes by  $\cos(\theta)$ .

$\theta$ : solar zenith angle

with normalization:



## 4 Physics-informed loss functions

Physics informed loss function:

$$Loss_2 = \frac{1}{N_{columns}} \sum_{n=1}^{N_{columns}} \|flux_{NN,n} - flux_{ecRad,n}\|^2 + \lambda \cdot penalty$$

Physics informed penalty:

1) Total column energy absorbed penalty:

$$\frac{1}{N_{columns}} \sum_{n=1}^{N_{columns}} \|(Netflux_{top} - Netflux_{surface})_{NN,n} - (Netflux_{top} - Netflux_{surface})_{ecRad,n}\|^2$$

2) Heating rates penalty:

$$\frac{1}{N_{columns}} \sum_{n=1}^{N_{columns}} \|\vec{HR}_{NN,n} - \vec{HR}_{ecRad,n}\|^2$$

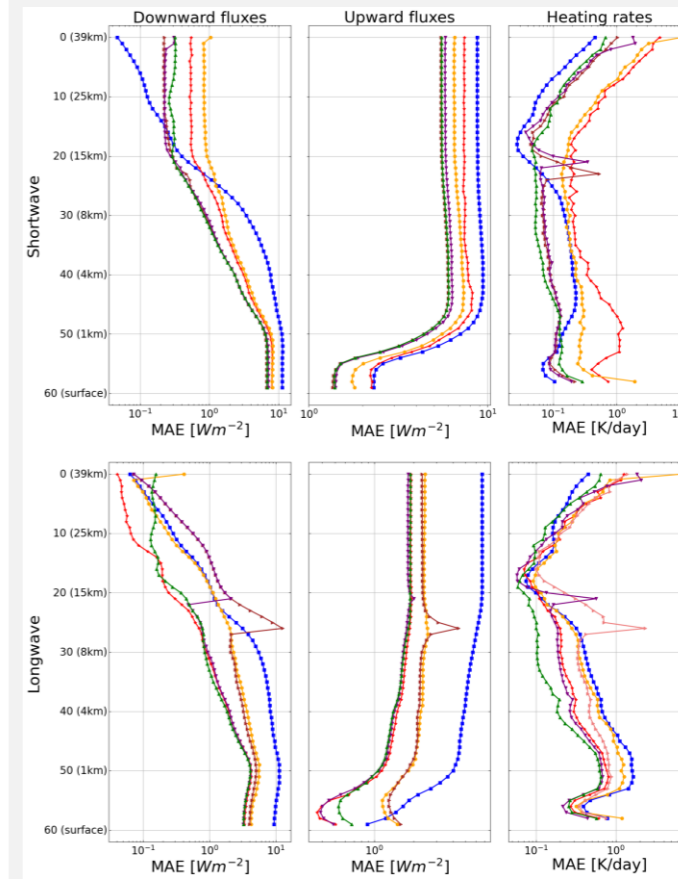
3) Height dependent heating rates penalty:

$$\frac{1}{N_{columns}} \sum_{n=1}^{N_{columns}} \sum_{h=59}^0 \alpha_h (HR_{NN,n,h} - HR_{ecRad,n,h})^2$$

$\alpha_h$  = average height in km at atmospheric level h

## 5 Results and outlook

MAE in the fluxes and heating rates:



Observation:

- For the total column energy absorbed penalty , the MLP learns to modify the top and bottom fluxes predictions to satisfy the additional penalty. This causes large heating rates MAE at the TOA and surface.
- We observe a large MAE at the tropopause for the MLP with HR penalty and .
- The random forest outperforms all NNs at the ToA for the heating rates predictions.
- The model we recommend is the UNet with height dependent heating rates penalty. It has neither an error kink at the tropopause nor a large jump in the error at the TOA. It is extremely accurate at all heights for both the fluxes and heating rates prediction.

Best model

Next step: Online performance

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